

**WORKING PAPER SERIES**



**OTTO VON GUERICKE  
UNIVERSITÄT  
MAGDEBURG**

**FACULTY OF ECONOMICS  
AND MANAGEMENT**

Impressum (§ 5 TMG)

*Herausgeber:*

Otto-von-Guericke-Universität Magdeburg  
Fakultät für Wirtschaftswissenschaft  
Die Dekanin

*Verantwortlich für diese Ausgabe:*

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*Bezug über den Herausgeber*  
ISSN 1615-4274

# Interjurisdictional Spillovers, Decentralized Policymaking and the Elasticity of Capital Supply\*

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September 15, 2010

## Abstract

This paper points to the important role which the elasticity of aggregate capital supply with respect to the net rate of return to capital plays for the efficiency of policymaking in a decentralized economy with mobile capital and spillovers among jurisdictions. In accordance with previous studies, we show that under the assumption of a fixed capital supply (zero capital supply elasticity) the decentralized policy choice is optimal. If the capital supply elasticity is strictly positive, however, capital tax rates are inefficiently low in the decentralized equilibrium.

JEL classification: H23, H77, Q58

key words: decentralized policymaking, spillovers, capital supply elasticity

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\*We would like to thank David Wildasin for useful comments. The usual disclaimer applies. Eichner: Department of Economics, University of Hagen, Universitätsstr. 41, 58097 Hagen, Germany, phone: ++ 49 (0) 2331 987 4141, fax: ++ 49 (0) 2331 987 4143, email: thomas.eichner@fernuni-hagen.de; Runkel: Faculty of Economics and Management, University of Magdeburg, Postbox 4120, 39016 Magdeburg, Germany, phone: ++ 49 (0) 391 67 18545, fax: ++49 (0) 391 67 11218, email: marco.runkel@ovgu.de.

# 1 Introduction

A key question in the Fiscal Federalism literature is whether decentralized policymaking in an economy with spillovers among jurisdictions leads to an efficient outcome (see e.g. Oates, 1974). A striking example where this question is of particular importance is the current debate on global warming. The failure of the Copenhagen Summit in late 2009 has impressively shown that centralized solutions to the climate change problem are hardly realizable. One might thus want to know whether a decentralized policy approach, where each country chooses its own climate policy without coordinating it with the climate policy of other countries, gives hope for an efficient policy outcome. Further important examples of decentralized decision making in the presence of interjurisdictional spillover effects can be found in the decentralized provision of education and infrastructure.

At first glance, it is hardly imaginable that decentralized policymaking can ever be optimal. It is not only the very existence of spillovers which causes doubt. Also the policy instruments themselves create (policy) externalities on other jurisdictions. Despite this presumption against the efficiency of decentralized policymaking, the previous literature provides several studies in which decentralization leads to an undistorted policy choice. An important example is given by Oates and Schwab (1988) who argue that the choice of capital tax rates in an economy with identical jurisdictions, mobile capital and local pollution may indeed be efficient. In a remarkable current paper, Ogawa and Wildasin (2009) extend the analysis to account for transboundary pollution (spillovers) and asymmetric countries, and still get the efficiency result. In their model emissions and, thus, the extent of spillovers generated by a jurisdiction is proportional to capital employed in this jurisdiction. The choice of capital tax rates is then distorted by the jurisdictions' incentive for tax competition and by the jurisdictions' ignorance of spillover effects. But the key argument is that both distortions just neutralize each other and thereby lead to efficient capital tax rates.

Our paper contributes to this literature and points to the important role which the elasticity of aggregate capital supply with respect to the net rate of return to capital plays for the efficiency of decentralized policymaking. In accordance with the previous literature, we show that under a fixed capital supply (zero capital supply elasticity) the decentralized policy choice is indeed optimal. If the capital supply elasticity is strictly positive, however, capital tax rates are inefficiently low in the decentralized equilibrium. The rationale is that, with a positive capital supply elasticity, a capital tax rate increase in one jurisdiction lowers

the net return to capital and, thus, aggregate capital supply as well as total emissions in the whole economy. For that reason the distortion of capital taxes due to the environmental spillover effects is smaller than in case with fixed capital supply and no longer large enough to compensate the distortion due to the tax competition incentive of the jurisdictions.

The paper is organized as follows. Section 2 describes the basic model assumption. In Section 3 we characterize the efficiency properties of decentralized policymaking, and Section 4 briefly concludes by discussing the relevance of a positive capital supply elasticity.

## 2 Model

**Firms.** We use a simplified version of the Ogawa and Wildasin (2009) model<sup>1</sup> and extend it to appropriately deal with elastic capital supply. Consider an economy with  $n$  jurisdictions. Jurisdiction indices are  $i, j \in \{1, \dots, n\}$  with  $i \neq j$ . In jurisdiction  $i$  there is a representative firm that employs  $k_i$  units of capital in order to produce  $F(k_i)$  units of an output good whose price is normalized to one. The production function is increasing and concave, i.e.  $F' > 0$  and  $F'' < 0$ . Each unit of capital is rented on the economy-wide capital market at the net return to capital denoted by  $\rho > 0$ . Since jurisdiction  $i$  levies a unit tax on capital at rate  $t_i$ , after-tax profit of the firm located in jurisdiction  $i$  reads

$$\pi_i = F(k_i) - (\rho + t_i)k_i. \quad (1)$$

The first-order condition of profit maximization is

$$F'(k_i) - t_i = \rho. \quad (2)$$

It equalizes the after-tax return to capital across countries.

**Households.** Each jurisdictions is populated by a representative household who lives for two periods. In the first period, jurisdiction  $i$ 's resident has an endowment  $\bar{k}$  of first period income that can either be spent for first-period consumption at rate  $x_i^1$  or saved at rate  $s_i = \bar{k} - x_i^1$ . In the second period, the resident receives capital income  $(1 + \rho)s_i$  and profit income  $\pi_i$  earned in her jurisdiction, less a lump sum tax  $\tau_i$  levied by jurisdiction  $i$ . The

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<sup>1</sup>The simplification is that we focus on the case of perfectly symmetric countries, while the analysis of Ogawa and Wildasin (2009) allows for country asymmetries. Abstracting from such asymmetries is suitable for our purposes since we are interested in the role of the capital supply elasticity.

second-period budget is  $x_i^2 = (1 + \rho)s_i + \pi_i - \tau_i$  where  $x_i^2$  denotes second-period consumption. Beside private consumption, utility of jurisdiction  $i$ 's resident is affected by the quantity  $g_i$  of a locally provided public good and by pollution  $e_i$ . The utility function is given by

$$u_i = U(x_i^1) + x_i^2 + V(g_i, e_i) = U(\bar{k} - s_i) + (1 + \rho)s_i + \pi_i - \tau_i + V(g_i, e_i). \quad (3)$$

The subutility functions  $U$  and  $V$  are assumed to be concave and satisfy  $U' > 0$ ,  $V_g > 0$  and  $V_e < 0$ . Maximizing utility (3) with respect to savings  $s_i$  gives  $U'(\bar{k} - s_i) - 1 - \rho = 0$ . This condition determines savings as a function of the interest rate  $\rho$ , i.e.  $s_i = S(\rho)$ . The derivative  $S'(\rho) = -1/U'' > 0$  serves as approximation for the capital supply elasticity  $\varepsilon := \rho S'/S$ . For notational convenience, we do not replace  $S'$  by an expression containing  $\varepsilon$ , but instead use  $S'$  to distinguish the case of a positive elasticity ( $S' > 0$  and  $\varepsilon > 0$ ) from the case of a zero elasticity, which is obtained by setting  $S' \equiv \varepsilon \equiv 0$ .

**Capital Market.** Capital is perfectly mobile. On the economy-wide capital market, capital demand of firms meets capital supply of households. The equilibrium condition is

$$\sum_{i=1}^n k_i = nS(\rho). \quad (4)$$

Equations (2) and (4) determine the equilibrium capital allocation  $\{k_i\}_{i=1}^n$  and the net return to capital  $\rho$  as functions of the tax rates  $\{t_i\}_{i=1}^n$ . Totally differentiating and then applying the symmetry property  $t_i = t$  and  $k_i = S(\rho)$  yields the comparative static results

$$\frac{\partial \rho}{\partial t_i} = -\frac{1}{n(1 - F''S')} < 0, \quad \frac{\partial k_i}{\partial t_i} = \frac{n - 1 - nF''S'}{n(1 - F''S')F''} < 0, \quad \frac{\partial k_j}{\partial t_i} = -\frac{1}{n(1 - F''S')F''} > 0, \quad (5)$$

$$\frac{\partial k_i}{\partial t_i} + (n - 1)\frac{\partial k_j}{\partial t_i} = -\frac{S'}{1 - F''S'} < 0. \quad (6)$$

As shown in (5), a unilateral increase in one jurisdiction's capital tax rate reduces investment in that jurisdiction and increases investment in all other jurisdictions via a decline in the net return to capital. The decisive difference of our approach to the case with fixed capital supply is that, according to (6), the increase in one jurisdiction's tax rate lowers total capital supply and, thus, total investment. Investment in the tax-increasing jurisdiction therefore falls by more than it does in the presence of a fixed capital supply. Formally, this is represented by the additional term  $-nF''S'$  in the numerator of  $\partial k_i/\partial t_i$  in equation (5).

**Emissions.** Each unit of capital employed in jurisdiction  $i$  generates  $\alpha > 0$  units of emissions in jurisdiction  $i$  and  $\beta\alpha$  units of emissions in jurisdiction  $j$ . The parameter

$\beta \in [0, 1]$  reflects the degree of interjurisdictional spillovers. In case of  $\beta = 0$  we have local pollution, while  $\beta > 0$  reflects transboundary pollution. The extreme case of  $\beta = 1$  approximates global pollution since each unit of emissions causes the same pollution in all jurisdictions. Total pollution in jurisdiction  $i$  is given by

$$e_i = \alpha k_i + \beta \alpha \sum_{j \neq i}^n k_j. \quad (7)$$

Differentiating (7) and taking into account (5) and (6) yields

$$\frac{\partial e_i}{\partial t_i} = \frac{\alpha[(1 - \beta)(n - 1) - nF''S']}{n(1 - F''S')F''} < 0, \quad \frac{\partial e_j}{\partial t_i} = \frac{\alpha[\beta - 1 - \beta nF''S']}{n(1 - F''S')F''} \begin{matrix} \geq \\ < \end{matrix} 0, \quad (8)$$

$$\frac{\partial e_i}{\partial t_i} + (n - 1) \frac{\partial e_j}{\partial t_i} = -\frac{\alpha[1 + \beta(n - 1)]S'}{1 - F''S'} < 0. \quad (9)$$

A tax rate increase in jurisdiction  $i$  induces a relocation of capital and, thus, emissions from jurisdiction  $i$  to all other jurisdictions. As a consequence, pollution in jurisdiction  $i$  falls if the 'spill back' effect is not perfect, i.e. pollution is not global ( $\beta \in [0, 1[$ ). Moreover, the increase in jurisdiction  $i$ 's tax rate reduces total capital supply and thereby total emissions according to (9). Hence, as shown by (8), pollution in jurisdiction  $i$  falls upon a tax rate increase in jurisdiction  $i$ , even if pollution is global ( $\beta = 1$ ). This property is an important difference to the world with fixed capital supply ( $S' \equiv 0$ ). It also explains why, according to (8), the effect of jurisdiction  $i$ 's tax rate on pollution in jurisdiction  $j$  is ambiguous. With a fixed capital supply ( $S' \equiv 0$ ), the relocation of capital and emissions raises (if  $\beta \in [0, 1[$ ) or leaves unchanged (if  $\beta = 1$ ) pollution in jurisdiction  $j$ . However, if capital supply is elastic ( $S' > 0$ ) and if the spillovers are strictly positive ( $\beta \in ]0, 1]$ ), jurisdiction  $j$  benefits from the additional reduction in investment and emissions in the tax-increasing jurisdiction  $i$ . Formally, this effect is reflected by  $-\beta nF''S'$  in the numerator of  $\partial e_j / \partial t_i$  in equation (8). Put differently, the more elastic capital supply, the lower is *ceteris paribus* the increase of pollution in jurisdiction  $j$  upon a tax rate increase in jurisdiction  $i$ . This effect will turn out to be the driving force behind our main insights derived below.

**Governments.** The government of jurisdiction  $i$  chooses the lump sum tax  $\tau_i$  and the capital tax  $t_i$  in order to maximize its resident's welfare (3). In so doing, it takes into account  $s_i = S(\rho)$ , (1), (2) and (4)–(9). Moreover, it is restricted by the budget constraint

$$g_i = t_i k_i + \tau_i, \quad (10)$$

where we assumed that the output of firms can be transformed one-to-one into the public good. Each government treats the policy variables of the other governments as given, so we consider a Nash policy game in the lump sum tax and the capital tax.

### 3 Decentralized Equilibrium

Focusing on the symmetric equilibrium with  $\tau_i = \tau^*$  and  $t_i = t^*$ , the first-order conditions of jurisdiction  $i$ 's welfare maximization are  $du_i/d\tau_i = 0$  and  $du_i/dt_i = 0$  or, equivalently

$$V_g = 1, \quad t^* = -\frac{\alpha[(1-\beta)(n-1) - nF''S']V_e}{n-1-nF''S'}. \quad (11)$$

The first condition in (11) shows that the lump sum tax is set such that the Samuelson condition for the optimal provision of public goods is satisfied. The second condition gives the equilibrium capital tax rate, which deviates from the full marginal damage a unit of emissions causes in the whole economy, i.e.  $t^* \neq -\alpha[1 + \beta(n-1)]V_e$ . This deviation is true independent of whether we consider fixed or elastic capital supply.

To assess the efficiency properties of the Nash equilibrium we determine the policy externalities, i.e. the effect of jurisdiction  $i$ 's tax rate on welfare in jurisdiction  $j$ . If the externality is positive (negative), then starting from the symmetric Nash equilibrium and marginally increasing the tax rates of all jurisdictions by the same amount leads to a Pareto improvement (deterioration) and, thus, the tax rates are inefficiently low (high). For a zero externality, the Nash equilibrium is efficient. Differentiating  $u_j$  from (3) with respect to  $\tau_i$  and  $t_i$  and taking into account (1), (2), (3)–(10) and the symmetry assumption yields

$$\frac{du_j}{d\tau_i} = 0, \quad \frac{du_j}{dt_i} = \text{FE} + \text{EE}, \quad (12)$$

with

$$\text{FE} = V_g \frac{\partial g_j}{\partial t_i} = -\frac{t^* V_g}{n(1-F''S')F''}, \quad \text{EE} = V_e \frac{\partial e_j}{\partial t_i} = -\frac{\alpha(\beta-1-\beta nF''S')V_e}{n(1-F''S')F''}. \quad (13)$$

According to (12), the equilibrium lump sum tax is efficient since the associated externality is zero. This is consistent with the Samuelson rule in (11). The cross-jurisdictional effect of the capital tax rate can be decomposed into two subexternalities. When jurisdiction  $i$  raises its capital tax rate, it does not take into account that capital flights out and thereby improves the tax base and public goods provision in jurisdiction  $j$ . This effect is reflected by the fiscal externality FE which is positive and points to inefficiently low tax rates. Second, if



jurisdiction  $i$  raises its capital tax rate, the associated relocation of capital changes pollution in jurisdiction  $j$ . This effect is captured by the environmental externality EE. Since  $\partial e_j / \partial t_i$  from (8) is ambiguous, the environmental externality is indeterminate in sign.

The decisive question is whether the sum of externalities is positive, negative or zero. Adding FE and EE and using the equilibrium conditions (11) yields

$$\frac{du_j}{dt_i} = \text{FE} + \text{EE} = -\frac{\alpha\beta n S' V_e}{n-1-nF''S'}. \quad (14)$$

From expression (14) we immediately obtain the following

**Proposition.** *Suppose the Nash policy game attains a symmetric equilibrium and pollution is transboundary, i.e.  $\beta \in ]0, 1]$ . If capital supply is fixed ( $S' \equiv 0$ ), then the equilibrium capital tax rate  $t^*$  is efficient. In contrast, if capital supply is elastic ( $S' > 0$ ), then the equilibrium capital tax rate  $t^*$  is inefficiently low.*

The first part of the Proposition replicates the efficiency result of Ogawa and Wildasin (2009). It is a remarkable result since, with mobile capital, the tax competition incentive of jurisdictions actually distorts the capital tax rate downwards. In the presence of interjurisdictional spillovers, however, the capital tax rate is distorted for a second reason. Each jurisdiction does not fully internalize the economy-wide environmental damage caused by its firm (remember  $t^*$  from (11)). The important contribution of Ogawa and Wildasin (2009) is to show that both distortions just neutralize each other, so equilibrium capital tax rates are efficient. In terms of externalities, with fixed capital supply the environmental externality EE is negative and just outweighs the positive fiscal externality FE.

The contribution of our analysis is the second part of the Proposition, which shows that with elastic capital supply the efficiency result does not longer hold. The driving force behind this result is the impact of the capital supply elasticity (approximated by  $S'$ ) on pollution. As argued in the discussion of (8), the larger the capital supply elasticity, the lower is the increase in jurisdiction  $j$ 's pollution upon an increase in jurisdiction  $i$ 's capital tax rate and, thus, the smaller is the distortion of the capital tax rate due to the ignored environmental spillover effects. Hence, if the capital supply elasticity is positive, the environmental distortion is no longer large enough to compensate the tax competition distortion. Put differently, with a positive capital supply elasticity the environmental externality EE in (13) is smaller in absolute terms than the fiscal externality FE in (13), hence the equilibrium capital tax rates become inefficiently low.

Two remarks are in order. First, it is the interaction of the positive capital supply elasticity ( $S' > 0$ ) and the existence of spillovers ( $\beta \in ]0, 1[$ ) which causes the inefficiency. With local pollution ( $\beta = 0$ ), the equilibrium capital tax rate is efficient even if capital supply is elastic. The reason why we need strictly positive spillovers is that the reduction of pollution in jurisdiction  $j$ , which causes the decisive decrease in the environmental externality, comes from the negative effect of the capital supply elasticity on investment and emissions in jurisdiction  $i$ , and this effect translates into a fall of pollution in jurisdiction  $j$  only if spillovers are strictly positive. Remember our discussion of equation (8). Second, an increase in the number of jurisdictions tends to aggravate the distortion of capital tax rates. From (14) we see that the policy externality which jurisdiction  $i$  inflicts on one single other jurisdiction becomes smaller as  $n$  increases. But the number of jurisdictions which are harmed by the ignorance of jurisdiction  $i$  increases. Hence, decisive is the sum of externalities inflicted on all other jurisdictions,  $(n - 1)(\partial u_j / \partial t_i)$ , and this sum is increasing in  $n$ . Roughly speaking, in economies with many relatively small jurisdictions the inefficiency therefore tends to be more severe than in economies with few relatively large jurisdictions.

## 4 Relevance

The assumption of a positive capital supply elasticity has intensively been used in the theoretical literature. An important example is the analysis of Keen and Kotsogiannis (2002) who point out that the relation of horizontal and vertical fiscal externalities in federal states crucially depends on the capital supply elasticity. Empirically, the evidence is mixed. A much-cited estimate for the capital supply elasticity is 0.4 found by Boskin (1978). Bernheim (2002) argues that the estimates range from values close to zero up to 0.4, whereas Gylfason (1993) reports estimated values significantly larger than one. Taking this mixed observations literally, our analysis can best be understood as complementing the previous literature. While the efficiency result of e.g. Ogawa and Wildasin (2009) is relevant for all economies where the capital supply elasticity has been found to be negligible, our analysis suggests that for economies with significantly positive capital supply elasticities it cannot be expected that decentralized policymaking yields an efficient outcome.

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